

4 Using R-K method of 4th order, solve
$$\frac{dy}{dx} = \frac{y^2 - x^2}{y^2 + x^2}$$
, y(0)=1 Find y(0.2) and y(0.4).

10M

OR

5 Solve the Laplace equation $u_{xx} + u_{yy} = 0$ given that







5M

5M

OR

7 Solve the D.E
$$\frac{d^2x}{dt^2} + 9x = \sin t$$
 using Laplace Transform given that
 $x(0) = 1, x\left(\frac{\pi}{2}\right) = 1$
UNIT-IV

8

a Prove that F[
$$x^n f(x)$$
] = $(-i)^n \frac{d^n}{dp^n} [F(p)].$ 5M

b Prove that
$$F_s \{ x f(x) \} = -\frac{d}{dp} [F_c(p)].$$

OR

9 Solve the integral equation
$$\int_{0}^{\infty} F(x) \cos px \, dx = \begin{cases} 1-p, 0 \le p \le 1 \\ 0, p > 1 \end{cases}$$
. Hence deduce that 10M

$$\int_{0}^{\infty}\frac{\sin^{2}t}{t^{2}}dt=\frac{\pi}{2}.$$

a Solve $(D^2 + 3DD' + 2D'^2)z = 24xy$.

UNIT-V

b Solve
$$\frac{\partial^3 z}{\partial x^3} - 2 \frac{\partial^3 z}{\partial x^2 \partial y} = 2e^{2x} + 3x^2 y.$$
 5M

OR

11 The points of trisection of a string are pulled aside through the same distance on 10M opposite sides of the position of equilibrium and the string is released from rest. Derive an expression for the displacement of the string at subsequent times and show that the midpoint of the string always remains at rest.